EXPLORATION

8-5 Dilations and Similarity in the Coordinate Plane

Use graph paper to explore similarity in the coordinate plane.

- **1.** Write down the vertices of $\triangle PQR$.
- 2. Multiply each coordinate of each vertex of $\triangle PQR$ by 3. Then graph $\triangle P'Q'R'$ with these new vertices. How is $\triangle P'Q'R'$ related to $\triangle PQR$?



- Now multiply each coordinate of each vertex of △PQR by ¹/₂. Then graph △P"Q"R" with these new vertices. How is △P"Q"R" related to △PQR?
- **4.** A *dilation* is a transformation that changes the size of a figure but not its shape. For a dilation with a *scale factor* of *k*, you can find the image of a point by multiplying each coordinate by $k: (a, b) \rightarrow (ka, kb)$. What is the scale factor of the dilation that mapped $\triangle PQR$ to $\triangle P'Q'R'$?
- **5.** What is the scale factor of the dilation that mapped $\triangle PQR$ to $\triangle P''Q''R''$?

THINK AND DISCUSS

6. Describe how to find the image of the point (12, -15) under a dilation with scale factor $\frac{2}{3}$.

EXPLORATION

8-5 Dilations and Similarity in the Coordinate Plane

Use graph paper to explore similarity in the coordinate plane.

- **1.** Write down the vertices of $\triangle PQR$. P(0, 4), Q(0, 0), R(2, 0)
- 2. Multiply each coordinate of each vertex of $\triangle PQR$ by 3. Then graph $\triangle P'Q'R'$ with these new vertices. How is $\triangle P'Q'R'$ related to $\triangle PQR$? $\triangle P'Q'R' \sim \triangle PQR$



- **3.** Now multiply each coordinate of each vertex of $\triangle PQR$ by $\frac{1}{2}$. Then graph $\triangle P''Q''R''$ with these new vertices. How is $\triangle P''Q''R''$ related to $\triangle PQR$? $\triangle P''Q''R'' \sim \triangle PQR$
- **4.** A *dilation* is a transformation that changes the size of a figure but not its shape. For a dilation with a *scale factor* of *k*, you can find the image of a point by multiplying each coordinate by $k: (a, b) \rightarrow (ka, kb)$. What is the scale factor of the dilation that mapped $\triangle PQR$ to $\triangle P'Q'R'$?
- **5.** What is the scale factor of the dilation that mapped $\triangle PQR$ to $\triangle P''Q''R''$? $\frac{1}{2}$

THINK AND DISCUSS

6. **Describe** how to find the image of the point (12, -15) under a dilation with scale factor $\frac{2}{3}$. Multiply each coord. by $\frac{2}{3}$: (8, -10).